

# The Synthetic Scale-up Data Generated by the Austin model and Their Estimation by the Kotake–Kanda Model

## \*Title of Manuscript

On the Similarity of Austin Model and Kotake–Kanda Model and Implications for Tumbling Ball Mill Scale-up

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## \*Keywords

*ball milling, breakage, population balances, Austin model, Kotake model, scale-up*

## \*Data Description

The Excel spreadsheet contains the synthetic scale-up data generated by the Austin model and their estimation using the Kotake–Kanda (KK) model, which overall yields the information presented in Table 2 of the manuscript. In view of all scale-up (SU) cases in Table 2, the Austin model, via Eqn. (12) of the manuscript, was used to produce the synthetic scale-up data, i.e., the specific breakage rate  $S_i^*$ , to which the  $S_i^*$  generated by the KK model, via Eqn. (13) of the manuscript, were compared (SU1–SU4 in Table 2). In SU1–SU4, standard values of the scale-up correction exponents, i.e.,  $N_1 = 0.5$  and  $N_2 = 0.2$ , were used. In SU5–SU8,  $N_1$  and  $N_2$  were estimated by fitting Eqn. (13) to the synthetic scale-up data for each diameter ratio  $D/D_T$  separately. In SU9–SU12, they were fitted to the synthetic scale-up data for all  $D/D_T$  data together. These two separate types of fits are presented in the Excel spreadsheet, which contains two separate spreadsheets entitled “Separately fitted” and “Simultaneously fitted.” For simplicity,  $S_i^*$  was replaced by  $S_i$  in the Excel spreadsheet. Columns A and B yield, respectively, the ball size  $d_B$  values and the particle size  $x_i$  values from which the artificial  $S_i$  values were calculated using the Austin model for different values of  $D/D_T$ . A summary table is included at the far right side of the Excel spreadsheet, which presents the values used in Table 2 of the manuscript.

## Nomenclature

$S_{i,A}$  and  $S_{i,K}$ :  $S_i^*$  calculated by the Austin model and estimated by the KK model

$S_{i,Kmod}$ :  $S_i^*$  estimated by the KK model with modified (fitted)  $N_1$  and  $N_2$

$\text{Sqrt}(S_{i,A})$  and  $\text{Sqrt}(S_{i,K})$ : Square root of  $S_{i,A}$  and  $S_{i,K}$

$\text{Sqrt}(S_{i,Kmod})$ : Square root of  $S_{i,Kmod}$

SE original: square error between the Austin and the KK model for  $N_1 = 0.5$  and  $N_2 = 0.2$

SE modified: square error between the Austin and the KK model for fitted  $N_1$  and  $N_2$

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